

Neuro-Symbolic Artificial Intelligence

Chapter 8

Neuro-Symbolic Programming

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Outline

- 1 End-to-end Differentiable Proving
- 2 Probabilistic Soft Logic

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End-to-end Differentiable Proving

End-to-End Differentiable Proving

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The problem

Inconsistent KBs

```

country("Austria").
capitalOf("Austria", "Vienna").
city("Wien").
country("Switzerland").
neighbor("Schweiz", "Austria").
capital("Suisse", "Berne").
city("Bern").
neighboring_capitals(Cap1, Cap2) :-
    capital(Ctr1, Cap1), capital(Ctr2, Cap2),
    neighbor(Ctr1, Ctr2), city(Cap1), city(Cap2),
    country(Ctr1), country(Ctr2).
?- neighboring_capitals("Switzerland", "Austria").

```

<https://github.com/mledoze/countries>

The solution

- Distinct symbols represent the same entities
`Österreich`, `Oesterreich`, `Austria`, `Autriche` → `Austria`
- Soft, parametric unification u_θ :
 - anything can unify with anything, e.g. `Österreich` with `Austria`
 - but every unification incurs a cost
 - as we go through the SLD tree, we keep the proofs with highest scores
- In detail:
 - Two variables $u_\theta(X, Y) \rightarrow$ score of 1 and $X=Y$
 - A variable and a constant $u_\theta(X, c) \rightarrow$ score of 1 and $X=c$
 - Two constants $u_\theta(a, b) \rightarrow$ score of $\exp(-\|\theta_a - \theta_b\|)$
- Every constant and every predicate a is represented by a high-dimensional, learnable vector θ_a
- The idea is that the vectors `Österreich`, `Oesterreich`, `Austria`, `Autriche` will end up close together

Rocktäschel & Riedel, *End-to-end Differentiable Proving*, NIPS 2017

Extensions

- Started as a PhD thesis in 2017
- Has been extended for
 - scalability (speed of inference + size of KB) ¹
 - use directly on natural language²
 - producing explanations³

¹Minervini *et al*, *Towards Neural Theorem Proving at Scale*, NAMPI@ICML 2018

²Weber *et al*, *NLProlog: Reasoning with Weak Unification for Question Answering in Natural Language*, ACL 2019

Minervini *et al*, *Differentiable Reasoning on Large Knowledge Bases and Natural Language*, Knowledge Graphs for eXplainable Artificial Intelligence 2020

³Bianchi *et al*, *Knowledge Graph Embeddings and Explainable AI*, Knowledge Graphs for eXplainable Artificial Intelligence 2020

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The problem

- For some problems, we can leverage structure, e.g. social and biological networks
- For some problems, we can leverage large amounts of data, e.g. the Web
- Structured models don't scale very well, so how do we leverage both?

The solution

Hinge-Loss Markov Random Fields and Probabilistic Soft Logic

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Bach et al, *Hinge-Loss Markov Random Fields and Probabilistic Soft Logic*, J. Mach. Learn. Res. 2017

The solution

- Rewrite Prolog-like rules into CNF, interpret them as objective functions
- Relax the resulting SAT problem using soft logic
- Use convex optimization to find the truth values (in $[0,1]$) for each grounded formula

Example

Knowledge base:

$$a(X) \leftarrow b(X).$$

$$a(c1).$$

$$b(c2).$$

Groundings + truth values:

$$a(c1) \quad x_1 = 1$$

$$a(c2) \quad x_2 \in [0, 1]$$

$$b(c1) \quad x_3 \in [0, 1]$$

$$b(c2) \quad x_4 = 1$$

Turning the rule into an objective:

- $a(c1) \leftarrow b(c1)$

- $a(c1) \vee \neg b(c1)$

- $\min\{1, x_1 + (1 - x_3)\}$ using Łukasiewicz logic

Full objective:

$$\operatorname{argmax}_{x_1, x_2, x_3, x_4} \min\{1, x_1 + (1 - x_3)\} + \min\{1, x_2 + (1 - x_4)\}$$

Actual objective: $\operatorname{argmax}_{x_2, x_3} \min\{1, 2 - x_3\} + \min\{1, x_2\}$

→ $x_2 = 1$ and the value of x_3 can be anywhere between 0 and 1.

Extensions

The package is called *Probabilistic Soft Logic (PSL)*

- It is well documented
 - Website⁴
 - Talks and tutorials
 - Wikipedia page
- It has been extended for scalability etc⁵

⁴<https://psl.linqs.org/>

⁵Magliacane *et al*, *foxPSL: A Fast, Optimized and eXtended PSL implementation*, Int. J. Approx. Reason. 2015

Extensions

It has been used in lots of applications

- Drug-drug interaction ⁶
- Entity resolution ⁷
- Recommender systems ⁸
- Stance prediction in online debates ⁹
- Knowledge graph inference ¹⁰

⁶Sridhar *et al*, *A probabilistic approach for collective similarity-based drug-drug interaction prediction*, Bioinform. 2016

⁷Bhattacharya & Getoor, *Collective entity resolution in relational data*, ACM Trans. Knowl. Discov. Data 2007

⁸Kouki *et al*, *HyPER: A Flexible and Extensible Probabilistic Framework for Hybrid Recommender Systems*, RecSys 2015

⁹Sridhar *et al*, *Joint Models of Disagreement and Stance in Online Debate*, ACL 2015

¹⁰Pujara *et al*, *Knowledge Graph Identification*, ISWC 2013