

# Logistique

- Jeudi soir je ferme les TP
- Inscrivez-vous avant jeudi pour le projet
  - Même titre pour 2 personnes dans le même groupe
- Les soutenances c'est vendredi 8h30 – 11h45 puis 13h30-15h
  - Votre présence est requise pendant toutes les soutenances
  - Temps de passage: 8 min de présentation, 5 min de questions

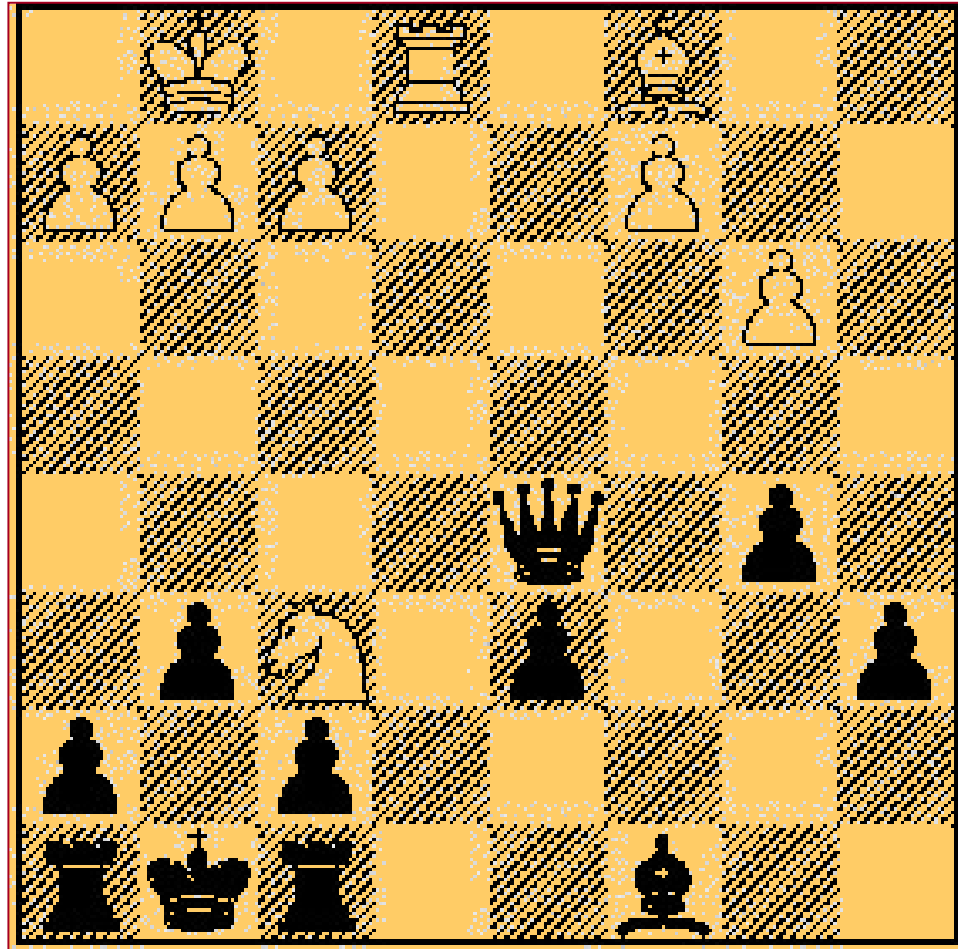
3EL05

Chapitre 5  
Complexité et cognition

# Contenu

- Structures
- Inattendu
  - Simplicité
  - Complexité causale
- Surprise et entropie de Shannon

# Structures

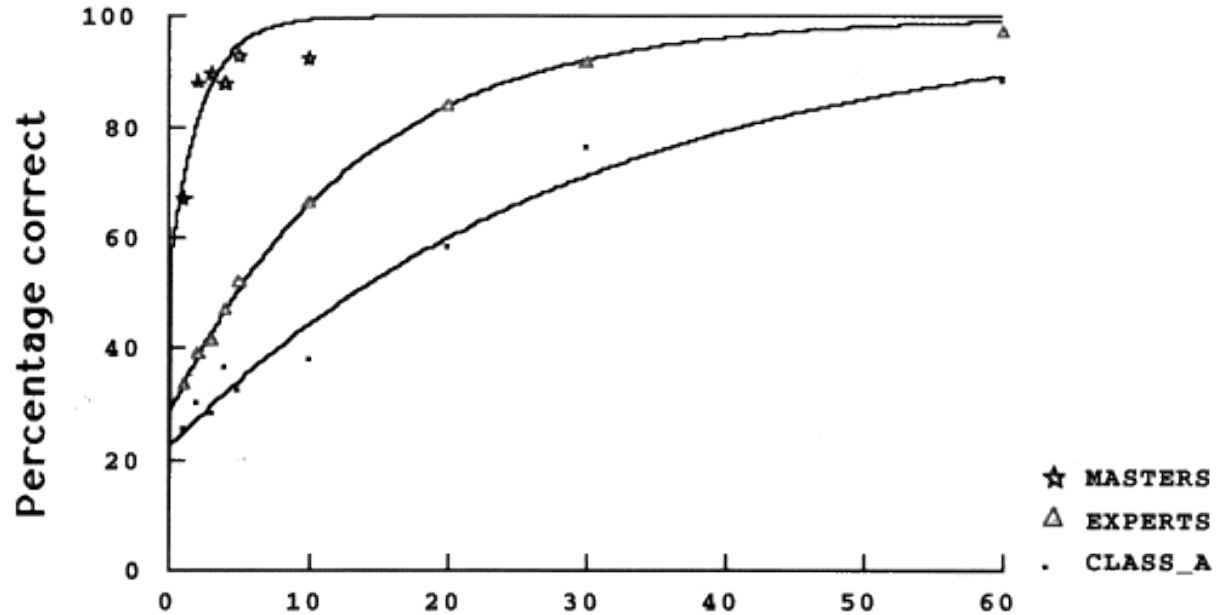


# Structures

Nineteen game positions were selected from various chess books with the following criteria: (a) the position was reached after about 20 moves; (b)

White is to move; (c) the position is "quiet" (i.e., is not in the middle of a sequence of exchanges); (d) the game was played by (Grand)masters, but is obscure. The mean number of pieces was 25.

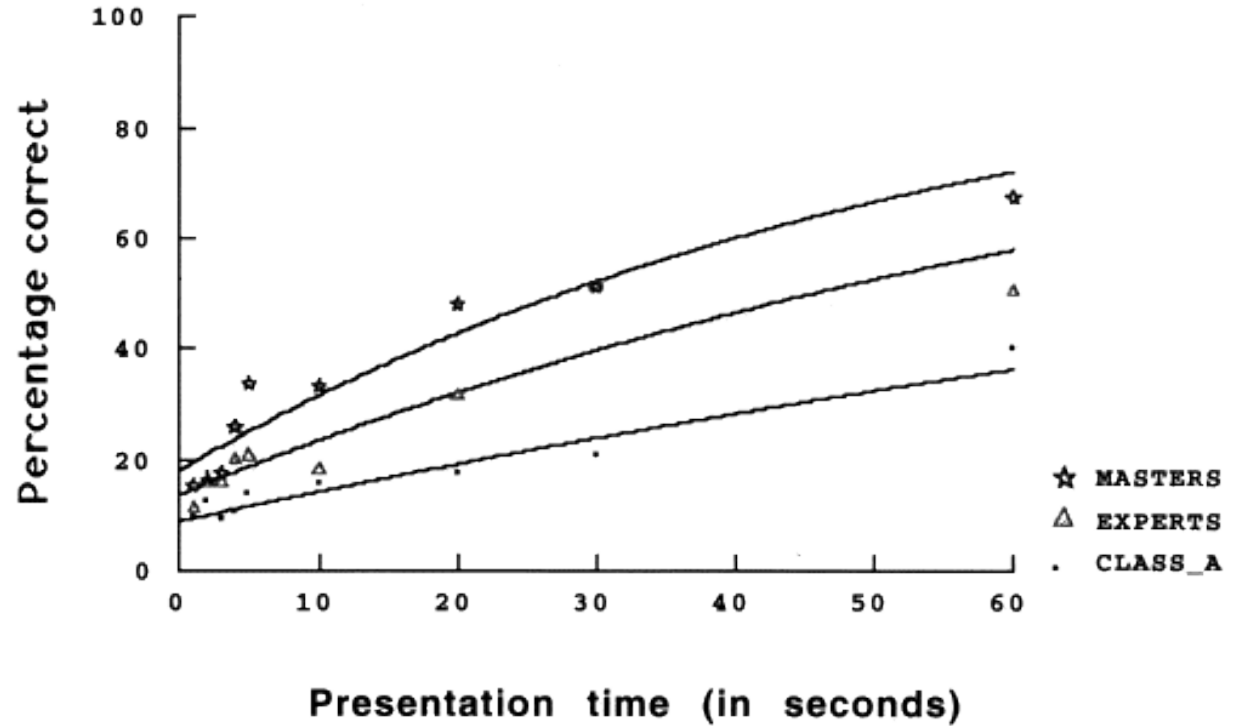
« Five seconds or sixty?  
Presentation time in expert  
memory »  
Fernand Gobet and Herbert A.  
Simon  
*Cognitive Science* 24(4), 2000,  
651-682



# Structures

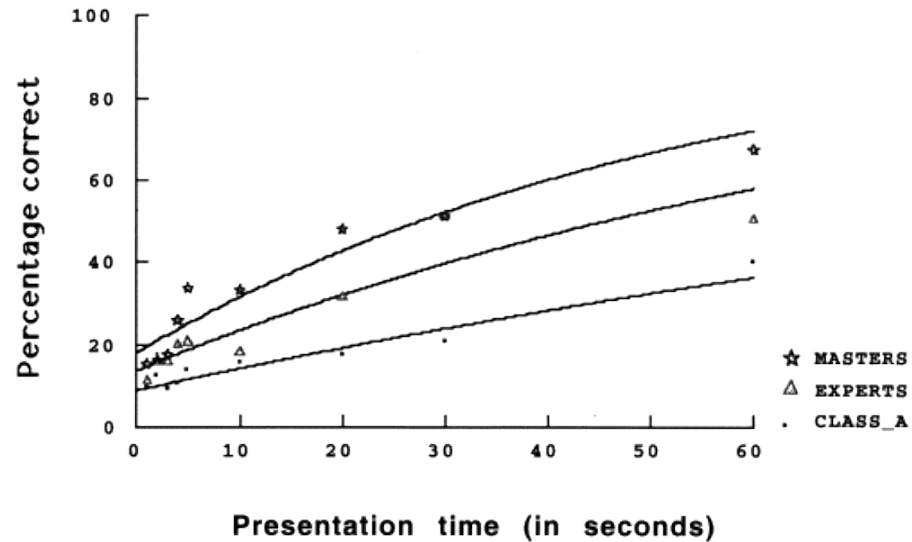
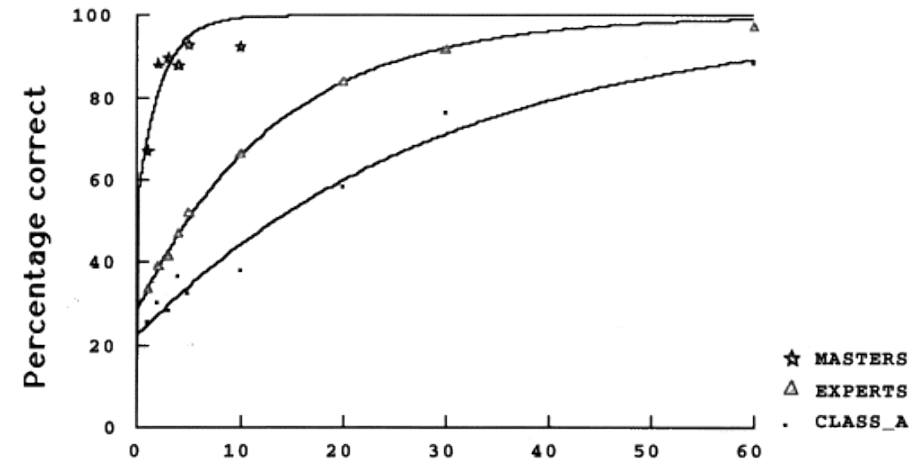
Ten random positions were created by assigning the pieces from a game position to random squares on the chessboard.

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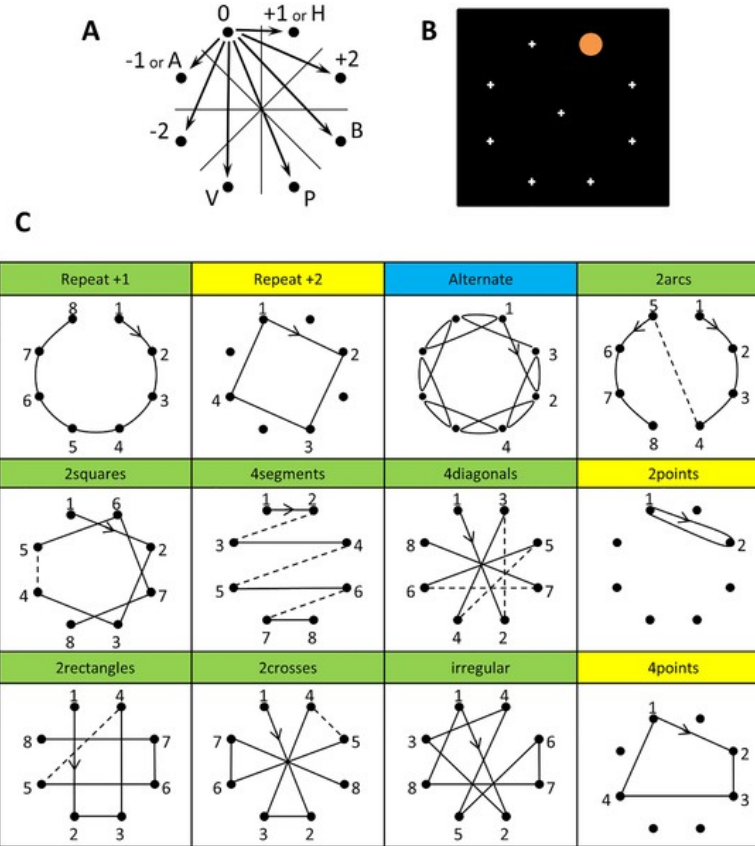


# Structures

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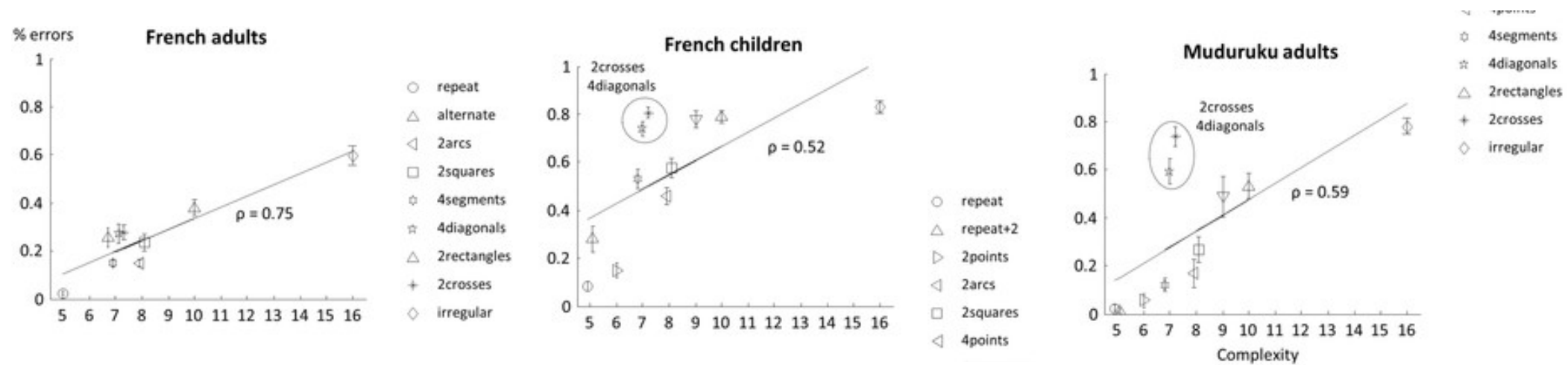
# Complexité et sciences cognitives



Amalric et al, *The language of geometry: Fast comprehension of geometrical primitives and rules in human adults and preschoolers*, PLOS Comp Bio 2017

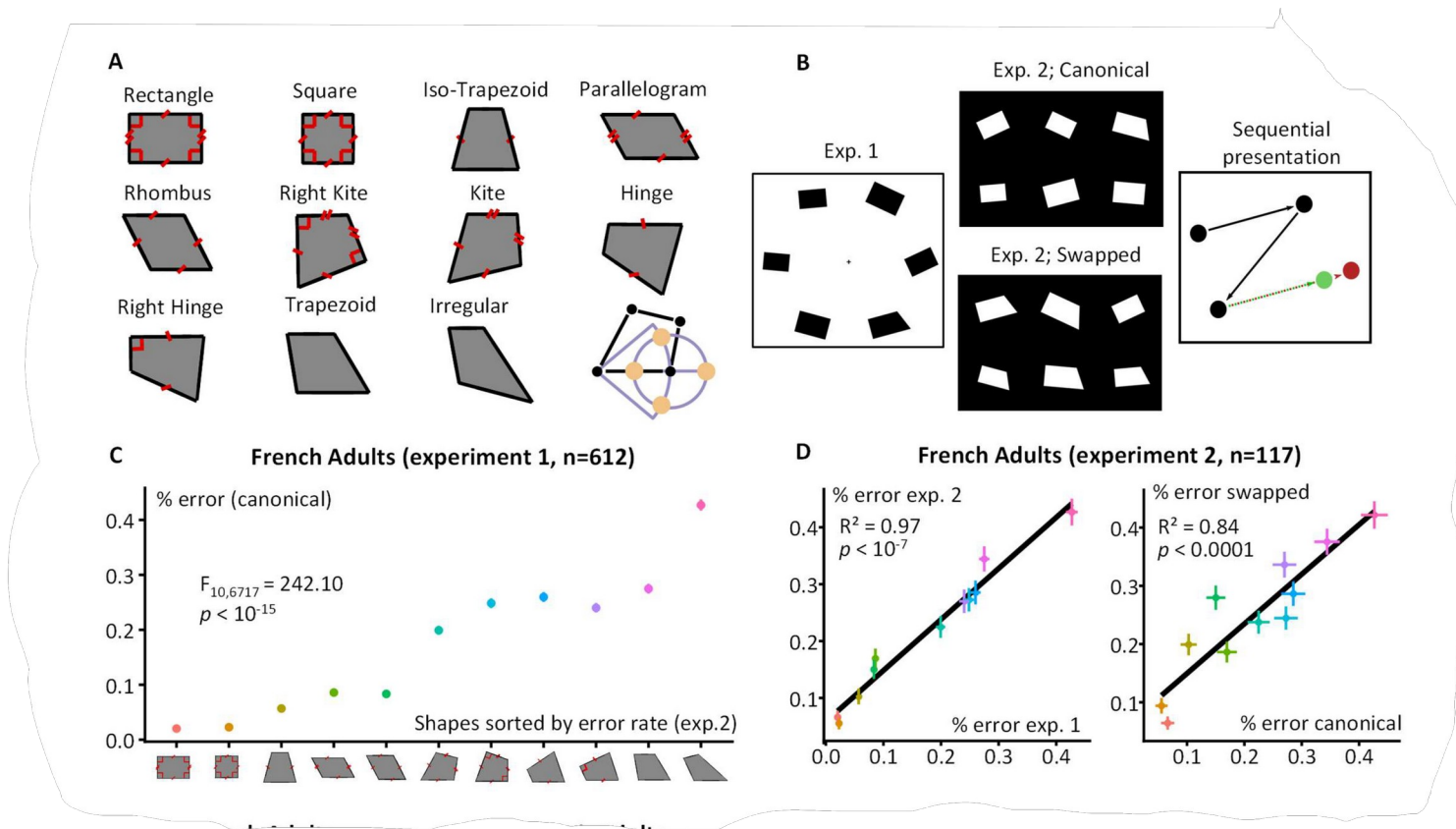


# Complexité et sciences cognitives



Amalric et al, *The language of geometry: Fast comprehension of geometrical primitives and rules in human adults and preschoolers*, PLOS Comp Bio 2017

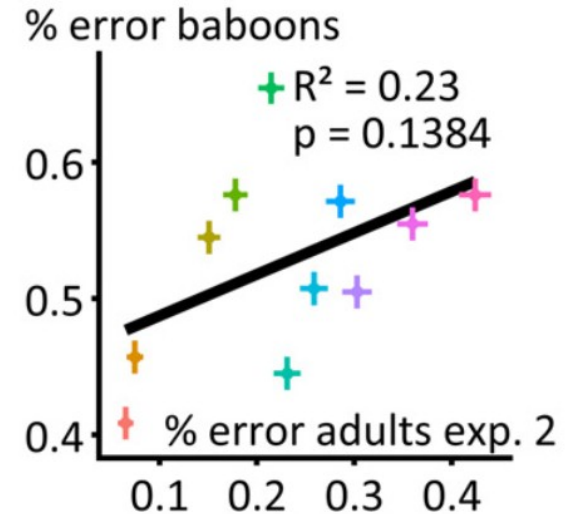
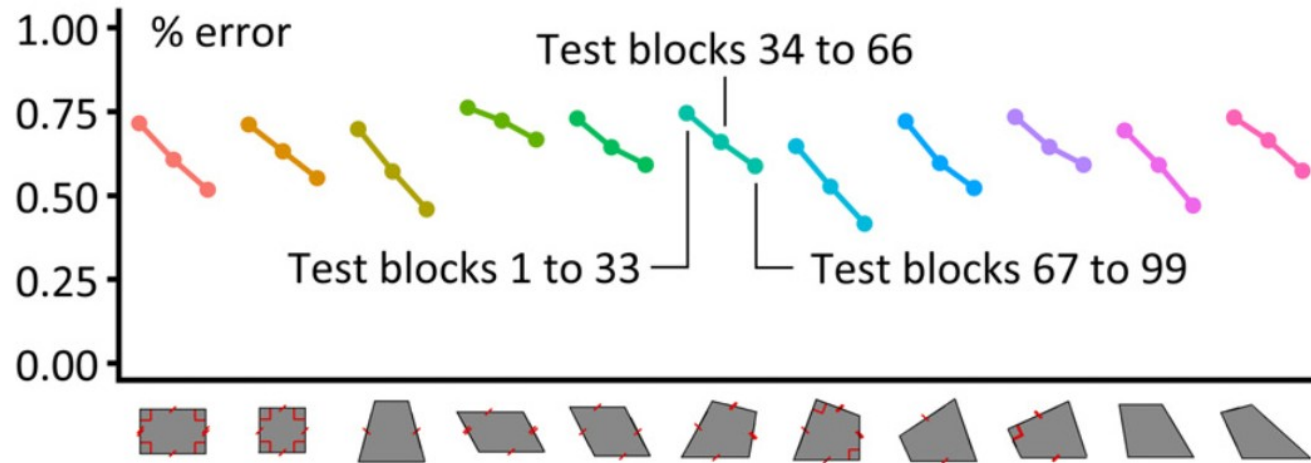
# Complexité et sciences cognitives



Sablé-Meyer et al, *Sensitivity to geometric shape regularity in humans and baboons: A putative signature of human singularity*, PsyArXiv 2020

# Complexité et sciences cognitives

Performance with geometric shapes



Sablé-Meyer et al, *Sensitivity to geometric shape regularity in humans and baboons: A putative signature of human singularity*, PsyArXiv 2020

# L'inattendu

- Soit un tirage de loto (6 nombres entre 1 et 99)
- Lequel est le plus inattendu/i
  - 1, 2, 3, 4, 5, 6
  - 42, 65, 2, 96, 22, 81

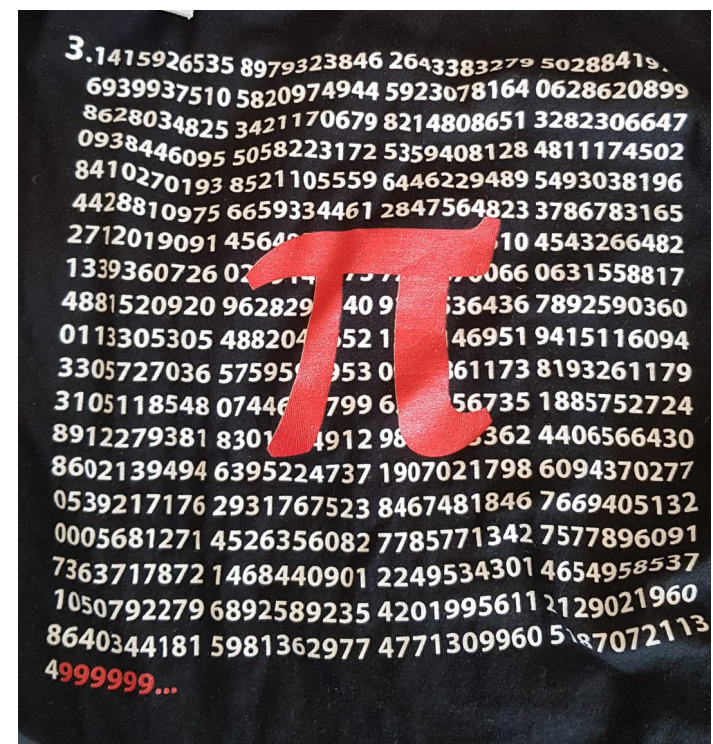


# L'inattendu

Famous physicist Richard Feynman was allegedly amazed at the occurrence of 6 nines at 762nd position in  $\pi$ 's decimal expansion.

His surprise is...

- ❑ legitimate because there is no regularity in pi's decimal expansion
- ❑ unfounded because any series of 6 numbers would have been equally likely at this position.



# L'inattendu

You travel far away from home  
and...

you bump into someone you know.

The event is certainly tweetworthy!

What would make you feel the urge  
to share the event even more?

- if the person is famous
- if the person is a close friend/colleague of yours
- if you meet them in a hard-to-reach place



# L'inattendu

L'inattendu est une différence positive entre la *complexité causale* et la *complexité descriptive*

$$U(s) = C_w(s) - C_d(s)$$

*complexité ex-ante*

*complexité ex-post*



# L'inattendu

- Calculer 2 complexités :
  - La complexité causale
  - La complexité descriptive
- Chacune utilise une machine différente :
  - Comment cet évènement a-t-il pu être généré par la machine “monde réel” ?
  - Comment cet évènement peut-il être décrit avec ma machine subjective ?



# L'inattendu

- Pour le loto :
  - La complexité causale  
Chaque tirage est équiprobable, il faut  $6 \log_2(99) \approx 39.8$  bits pour le générer
  - La complexité descriptive dépend du tirage
    - Pour 42, 65, 2, 96, 22, 81 c'est presque  $6 \log_2(99)$  bits
    - Pour 1, 2, 3, 4, 5, 6 c'est beaucoup moins, peut-être  $\log_2(6) + C(\text{"compter"})$

L'inattendu *the occurrence of 6  
nines at 762nd  
position in  $\pi$ 's  
decimal expansion*

- Pour les décimales de  $\pi$  :

- La complexité causale

Chaque suite est équiprobable, il faut  
bits pour la générer

- La complexité descriptive

$$C(\pi) + C(9) + C(6) + C(762)$$



$\approx 15.3$  bits

Si vous êtes scientifique,  
cette complexité est faible

# Complexité et entropie

$N_1$  red balls

$N_2$  blue balls

$$N = N_1 + N_2$$

One draw:  $s$

$n_1$  red balls

$n_2$  blue balls

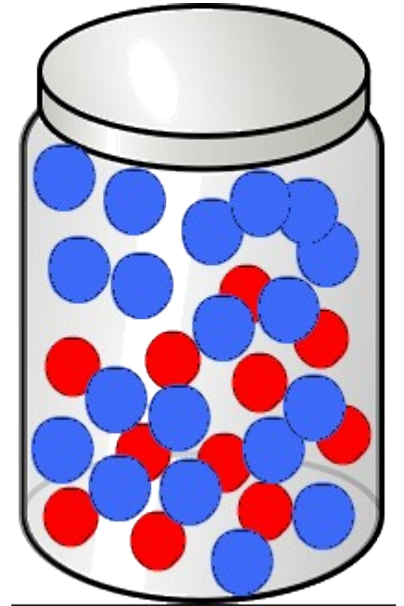
$$n = n_1 + n_2$$

Color of balls is unknown ex-ante

Ex-ante complexity:

Ex-post complexity

Surprise:



# Complexité et entropie

$N_1$  red balls

$N_2$  blue balls

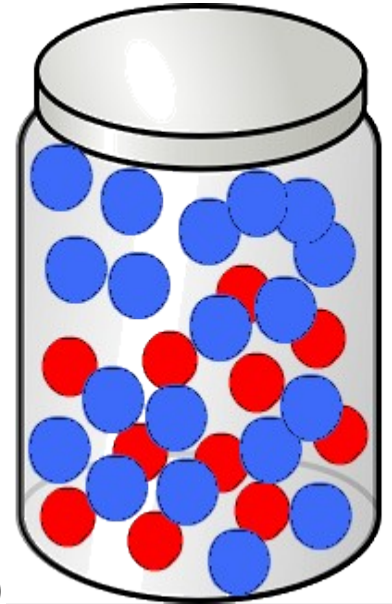
$N = N_1 + N_2$

One draw:  $s$

$n_1$  red balls

$n_2$  blue balls

$n = n_1 + n_2$



Color of balls is unknown ex-ante

Ex-ante complexity:  $C_w(s) = n \log(N)$

if  $N \gg n$  or if balls are put back

Ex-post complexity:  $C(s) = n_1 \log(N_1) + n_2 \log(N_2)$  (if order is 'random' or ignored)

Surprise:  $U(s) = C_w - C = -n [(n_1/n) \log(p_1) + (n_2/n) \log(p_2)]$

where  $p_i = N_i/N$  prob. of drawing a ball with colour  $i$

When  $n_i/n = p_i$ , we have  $U(s)/n = H(s)$

$U(s)/n - H(s) = KL(s)$

average unexpectedness  $\geq$  entropy

Cross-entropy

# Complexité et entropie

$$I(s) = -\log_2(p(s))$$

$$p(s) = 2^{-K(s)}$$

Claude Shannon

Ray Solomonoff

# L'inattendu

Vous rencontrez quelqu'un dans un endroit loin de chez vous...

$$U(s) = C_w(s) - C_d(s)$$

- Est-ce un endroit où passe beaucoup de monde ?
- Est-ce que cette personne avait une raison évidente d'être là ?



- Cette personne est-elle facile à décrire pour vous ?
- En haut de votre liste de personnes importantes ?
- Connue de nombreuses autres personnes ?

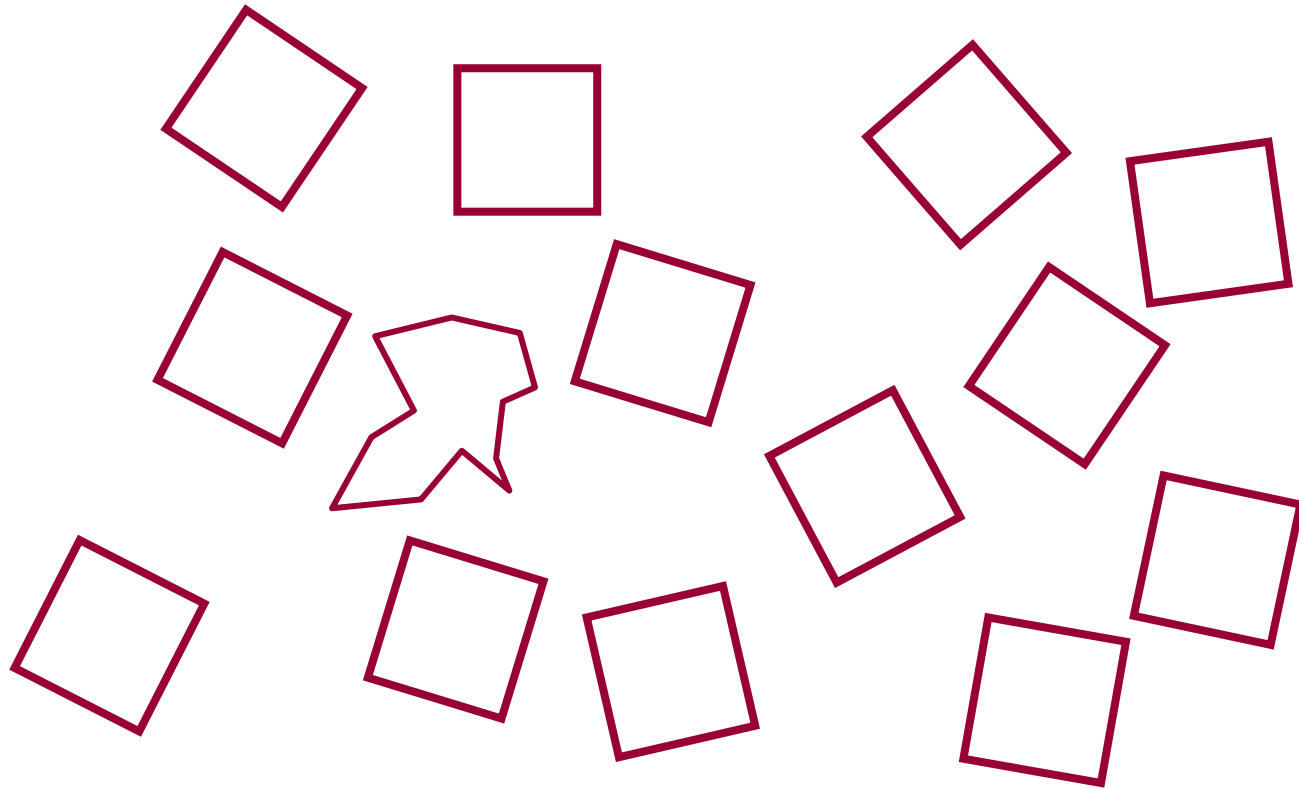
# Les tours de magie



Complexité causale élevée : comment expliquer qu'un lapin se retrouve dans un chapeau ?

Complexité descriptive faible : Un lapin. Dans un chapeau.

# Les anomalies





# Les coïncidences

Lincoln was elected to Congress in 1846, Kennedy was elected to Congress in 1946.

Lincoln was elected president in 1860, Kennedy was elected president in 1960.

Both presidents have been shot in the head in presence of their wives.

Both successors were named Johnson, born in 1808 and 1908.

Kennedy was shot in a car named Lincoln

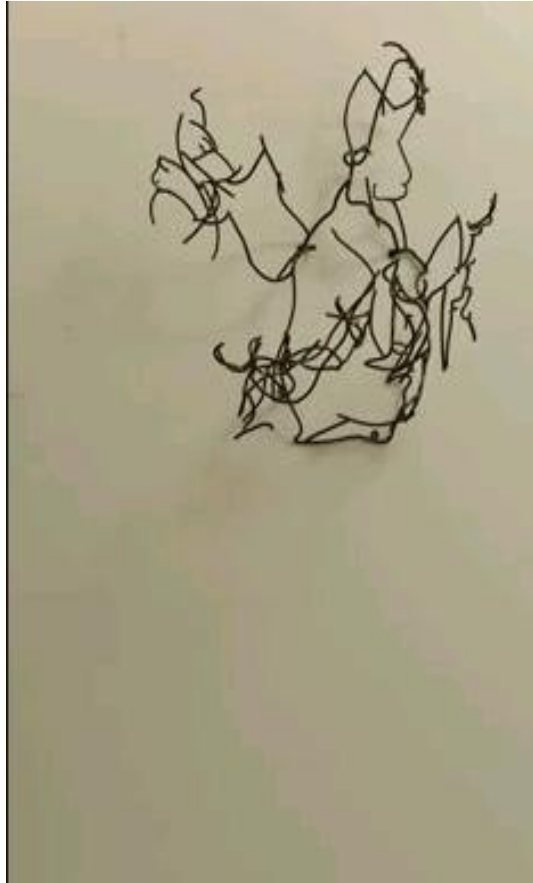
Both assassins were assassinated before their trials

$$C(\text{Lincoln}) + C(\text{Kennedy}) - C(\text{Lincoln}, \text{Kennedy})$$



Solution: Probability has virtually nothing to say about coincidences. Coincidences are explained by *complexity drop*. Each element  $x_i$  common to the two situations requires  $2 \times C_w(x_i)$  bits to be generated (e.g. the complexity of choosing the vice president's name). But it needs to be described only once  $\rightarrow$  hence the compression. The 100 year shift costs less to be described than, say, 84. Famous people cost less on the description's side as well (much less than e.g. two obscure Guatemalan presidents).  
Related topic: Analogies correspond to minimal complexity.

# L'esthétique



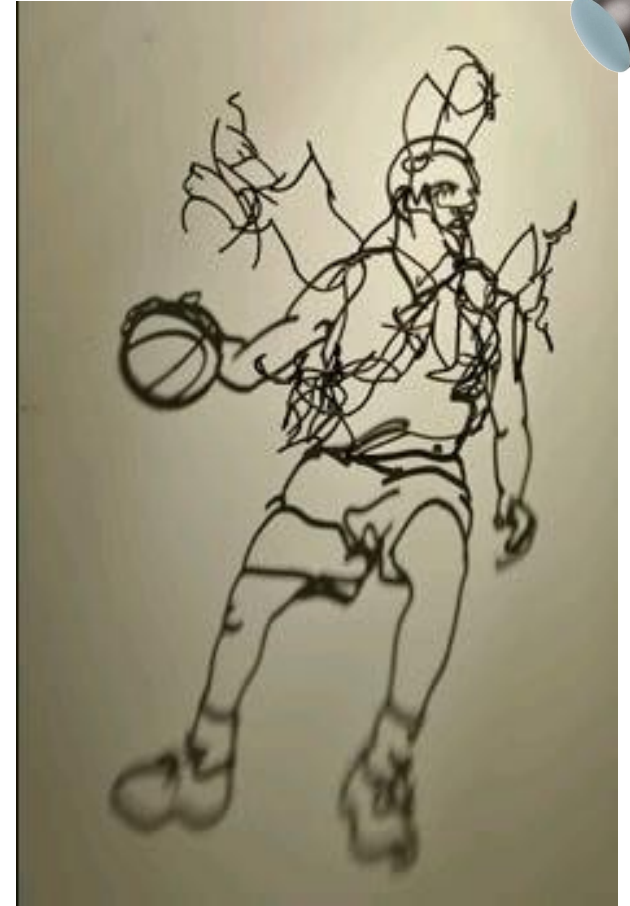
Complexité *ex-ante*  
de l'ombre

VS

Complexité *ex-post*  
de l'ombre



Larry Kagan



# Complexité, responsabilité et culpabilité

## Chapitre 4

Un robot capable de calculer sa  
responsabilité  
sera-t-il responsable de ses actes?

Jean-Louis Dessalles  
Telecom-Paris

*Responsable mais pas coupable*

## A Computational Model of Moral and Legal Responsibility via Simplicity Theory

Giovanni SILENO<sup>a,1</sup>, Antoine SAILLENFEST<sup>b</sup> and Jean-Louis DESSALLES<sup>a</sup>  
<sup>a</sup>*LTCI, Télécom ParisTech, Université Paris-Saclay, 46 rue Barrault, Paris, France*  
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**Abstract.** Responsibility, as referred to in everyday life, as explored in moral philosophy and debated in jurisprudence, is a multiform, ill-defined but inescapable notion for reasoning about actions. Its presence in all social constructs suggests the existence of an underlying cognitive base. Following this hypothesis, and building upon *simplicity theory*, the paper proposes a novel computational approach.

**Keywords.** moral responsibility, legal responsibility, simplicity theory, foreseeability, inadvertence, risk, negligence

Dessalles, J.-L. (2021). In G. Aïdan & D. Bourcier (Eds.), *Humain non-Humain - Repenser l'intériorité du sujet de droit*, 47-56. Paris: Librairie LGDJ.

# L'attendu

$$U(s) = C_w(s) - C_d(s)$$

Cas où  $U(s) < 0$  ?

# Conclusion

- La complexité explique de nombreux phénomènes cognitifs, avec un minimum de modélisation
- Le cerveau humain est-il capable de calculer une forme de complexité ?

## Opinion

Symbols and mental programs: a hypothesis about human singularity

# Conclusion du cours

- La complexité et l'information algorithmique infusent :
  - Les mathématiques
  - L'apprentissage automatique
  - Les sciences cognitives
- Découvrir la complexité m'a causé une chute de complexité (= j'ai mieux compris le monde)
- J'espère que pour vous aussi